



Temporal Characteristics of Debris Flow Surges

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Debris flow is one of the most destructive geomorphological events in mountainous watersheds, which usually appears in the form of successive surge waves as observed all over the world. In particular, debris flows in the Jiangjia Gully in southwest China have displayed a great variety of surge phenomena; each debris flow event contains tens or hundreds of separate surges originating from different sources. Therefore, the surge sequence of an event must encode the information of debris flow developing. The unmanned aerial vehicle photos provide an overview of debris flow sources, showing the different potentials of the debris flow and surge sequences present various patterns responding to the rainfall events. Then the variety of rainfalls and material sources determine the diversity of surge sequence. Using time series analysis to the surge discharge sequences, we calculate the Hurst exponent, the autocorrelation function, and the power spectrum exponent and find that all the sequences commonly share the property of long-term memory and these parameters are correlated in an exponential form, with values depending on rainfall patterns. Moreover, all events show a gross trend of discharge decay, despite the local rainfall process, which implies the intrinsic nature of the surge sequence as a systematic behavior of watershed. It is expected that these findings are heuristic for establishing mechanisms of debris flow initiation and evolution in a watershed.

Keywords: stationary, persistence, long-term memory, Hurst exponent, debris flow

INTRODUCTION

Debris flow occurs frequently in mountainous watersheds (Huerlimann et al., 2006; Deangeli et al., 2011). Three factors are key to the occurrence of a debris flow: steep topography, high-intensity rainfall, and abundant loose debris (Lin et al., 2002). Initially developed from randomly distributed tributaries (Li et al., 2004), debris flow is a full-valley process that finally converges into the downstream channel (Liu et al., 2008; Liu et al., 2009). It moves rapidly and strongly entrains material and water from the flow path (Iverson and Vallance, 1997; Hürlimann et al., 2003; Berti and Simoni, 2005; Godt et al., 2007; Cui, 2015; Hung et al., 2014). Sometimes, debris flow may temporarily dam rill channels, creating new rills or plunge pools, and quickly change into hyper concentrated flow when mixed with additional water from overland flow (Godt et al., 2007). Heavy rainfall facilitates the running process of debris flows by increasing pore water pressure, seepage force, and reducing effective stress of soils (George et al., 2007). Loose debris includes loose mud, sand, soil, and rock

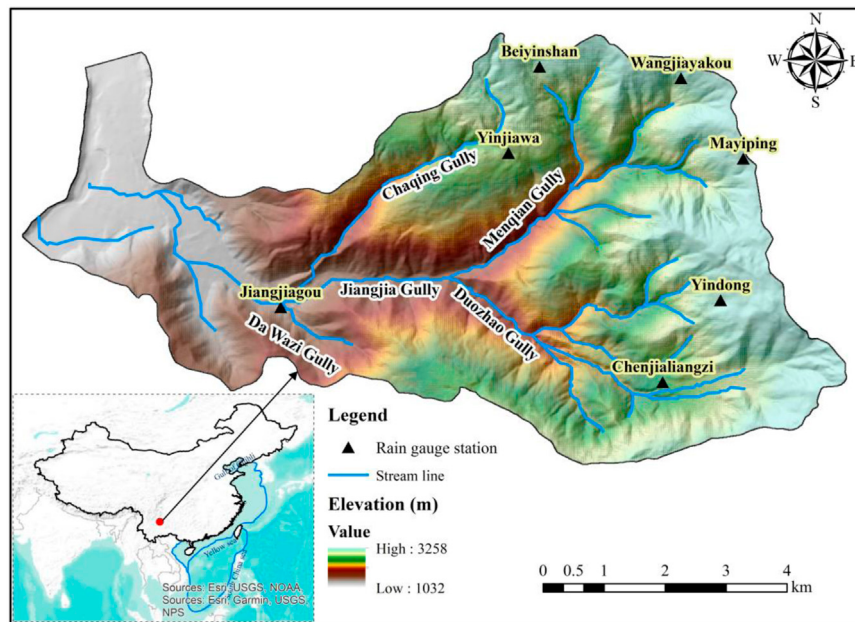


FIGURE 1 | Digital elevation model and the distribution of rain gauges in Jiangjia Ravine.

(Jakob and Hungr, 2007). The local rainfall and the material sources together influence the occurrence and fluctuation of debris flows.

A conspicuous phenomenon is that debris flow emerges in the form of separate surge waves (Liu et al., 2008; Liu et al., 2009). A surge is wave-like locomotion of high-density liquid restricted to a certain volume and spatial shape (Liu et al., 2009). A typical surge has a steep front or “head” with the densest slurry, the highest concentration of boulders, and the greatest depth, and it is followed by a progressively more dilute and shallower “tail” (Hungr, 2000). Surges are found to originate from the varieties of tributaries and discontinuities in mass supplies (Wu and Kang, 1993; Li et al., 2004; Ni and Lu, 2005; Liu et al., 2008; Liu et al., 2009), and a debris flow event always contains tens or hundreds of surges. Therefore, a surge sequence must embody with information of debris flow forming and developing from tributaries to the mainstream. Surges come from different tributaries and undergoing different processes (Liu et al., 2009), and time intervals between different surges during one debris flow event varies from 1 to 10^3 s. Besides, the appearances of surges reflect their sources and originations.

Former research concerning debris flows includes systematic investigation of debris flow hazards and related phenomena (Lin et al., 2002; Huerlimann et al., 2006; Jakob and Hungr, 2007), debris flow susceptibility (Dong et al., 2010; Kappes et al., 2011), geological factors inducing debris flows (Chen and Su, 2001), the relationship between rainfall and debris flows (Guzzetti et al., 2008), etc. In this study, we research debris flows that occurred in the JJG as debris flows in this area are well known for their high frequency and variety of surge appearances, and a long-term continuous monitoring and field observation in this watershed have provided a huge dataset of surge parameters. Based on the

data, this study attempts to find the temporal characteristics of surge sequence as a time series and their association with the forming conditions of rainfall and material sources. At first, we provide an overall view of JJG and its debris flow appearances; then we display the surge sequences in various patterns under different rainfall conditions; finally, we analyze the time series of the surge sequences to reveal their temporal features, which are believed to help understand the developing of debris flow in the valley scale.

DATA AND METHODS

Description of the Study Area

The research area JJG, one of the main gully located in the Jiangjia Ravine watershed (between $N26^{\circ}13' \sim N26^{\circ}17'$, and $E103^{\circ}06' \sim E103^{\circ}13'$, 48.6 km^2), is a tributary of the Jinsha River with the trunk channel length of 13.9 km and is situated 200 km northeast of Kunming, the capital of the Yunnan Province (Figure 1). The JJG is developed in the zone of the Xiaojiang fault, of which two-branched joins in the downstream reaches (Peng et al., 2005). With favorable climate (long-duration low-intensity precipitation in rainy seasons), topography (widespread steep-slope tributaries), and geographical factors (unconsolidated regolith), debris flows frequently occur here. The frequencies of debris flow in JJG can reach as many as 28 episodes in a single year (Peng et al., 2005). Debris flows here have characters of conspicuous fluctuation, viscous flow, and variety of appearances (Chen et al., 2005; Yong et al., 2012). In this research, we use data for 40 debris flow discharge series collected from the Dongchuan Observation and Research Station. The discharge of a surge is estimated by the product of the flow velocity between the fixed sections and the

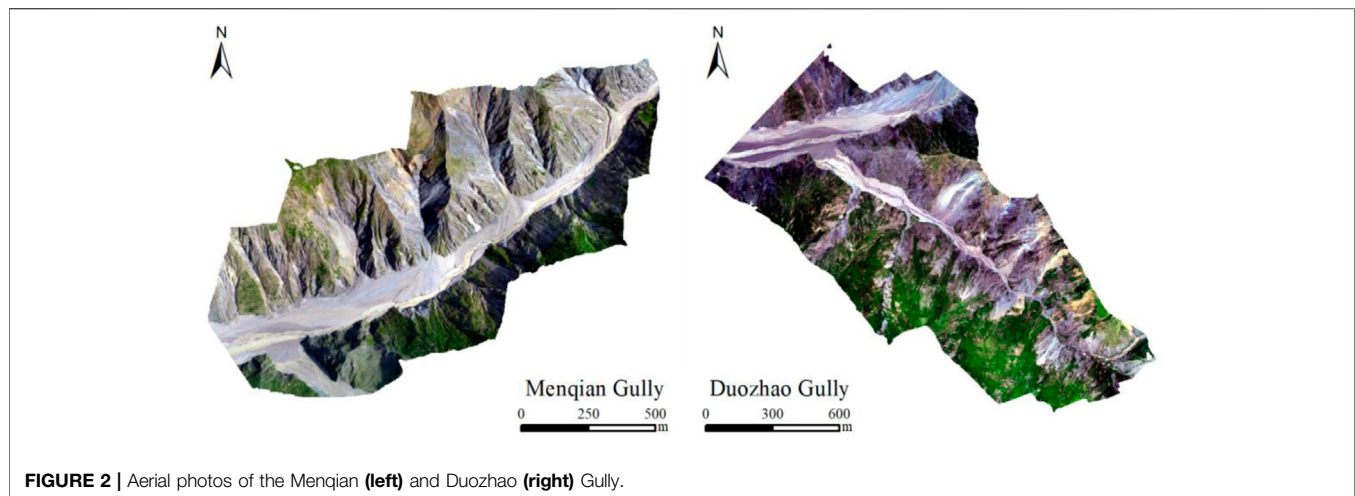


FIGURE 2 | Aerial photos of the Menqian (left) and Duo Zhao (right) Gully.

average section area (Kang et al., 2006). The temporal interval between successive surges ranges from tens to hundreds of seconds (Liu et al., 2009). The ID of each series denotes the date of the event, for instance, “070724” indicates the debris flow that occurred on July 24, 2007.

Precipitation Data Collection

Local rainfall occurs mainly between May and October and average rainfall gauges between 400–1,000 mm (Xiao-junGuo, et al., 2013). There are nine rain gauges locate in JJG (Figure 1) with precision of 0.1 mm and temporal resolution of 1 min. As data being collected from different rainfall gauges show little variance, we use data from Mayiping for its continuous and complete character.

Debris Flow Data Collection

In this research, we use data for 40 debris flow discharge series collected from the Dongchuan Observation and Research Station, Chinese Academy of Sciences. Measuring quantities include the debris flow discharge (m^3/s), the flow depth (m), the velocity (m/s), the flow density (m^3/s), the time interval (s), etc. The discharge of a surge is estimated by the product of the flow velocity between the fixed sections and the average section area (Kang et al., 2006). The flow depth is directly read from the level mark inscribed on concrete pile at the section. The velocity is measured as an average value of the surge passing through two fixed cross sections (Li et al., 2015). The flow density is determined directly by weighing the fluid. The temporal interval between successive surges ranges from tens to hundreds of seconds (Liu et al., 2009). The ID of each series denotes the date of the event, for instance, “070724” indicates the debris flow that occurred on July 24, 2007.

RESULTS AND DISCUSSION

Environmental Conditions and Debris Flows

As being mentioned in the introduction part, material sources, geography, and precipitation are all factors that influence the initiation and moving of debris flows.

Material Sources, Geography, and Debris Flows

Field surveys have indicated that debris flows in JJG originate almost from one of the major tributaries, the Menqian Gully; while the other tributary, Duo Zhao, has few occurrences. Through filed investigation, we found out that Menqian has 65 major tributaries ($>0.1 \text{ km}^2$) and Duo Zhao has 76 dendritic tributaries. As shown in Figure 2, the tributary structure and material sources are remarkably different in these two gullies. This controls the initiation and development of debris flow surges. Moreover, material sources differ much in the two gullies. Based on field surveys, it is estimated that material quantity from potential landslides and streambed sediment is about $5.2 \times 10^8 \text{ m}^3$ in Menqian and $2.3 \times 10^8 \text{ m}^3$ in Duo Zhao.

The trigger mechanism of debris flow in JJG usually takes place in two stages: the primary slope failure in the source area, and the hydraulic movement which transfers the solid materials flowing into the brook track (Lee et al., 2008). A typical debris flow event includes three processes: initiation in the source area, transportation along tributaries and main gullies, and debris accumulation in the end. Figure 3 exhibits the three processes: the initiation (A), the transportation (B), and the accumulation (C) stage. The source area of each debris flow event has a scar appearance (Figure 3A) with peeling land surface and erosive gully. Then rainfall soaks down into the debris, adds weight, and triggers a flow (Takahashi, 2014). Debris flows move in the form of surges (Figure 3B) due to the varieties of tributaries and the discontinuities in mass supplies. For instance, a debris flow event occurred on July 7, 2017 (170707), which started at 3:50:52 in the morning and ended at about 8:00:00 in the evening, carrying $5.78 \times 10^4 \text{ m}^3$ of the sediment. Throughout this event, there appears individual 38 surges with average time intervals being 65 s. Each debris flow event consists of tens or hundreds of surges separated in time. During the debris motion in the valley, the transportation (Figure 3B) and accumulation process (Figure 3C) of the debris flow are controlled by the high potential for grain crushing of deposits upstream and lower potential for the deposits downstream.

Debris flows move down hillslopes (Figure 3C) across unobstructed fan surfaces in almost any direction and

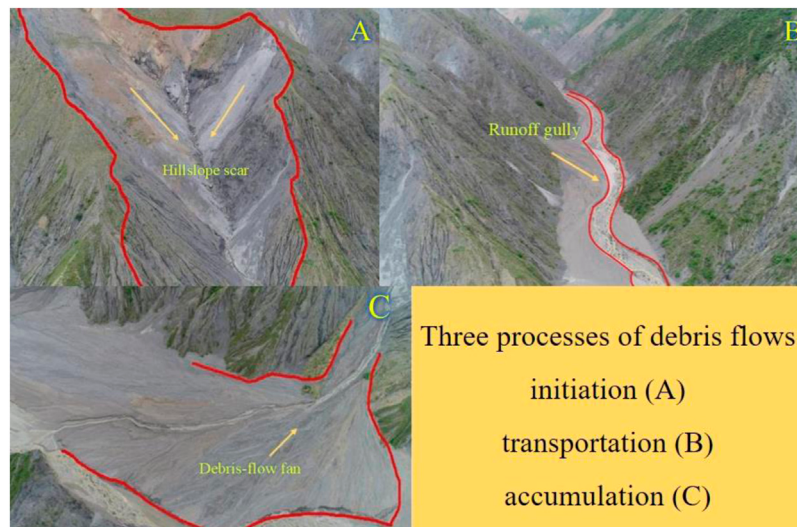


FIGURE 3 | Three processes of debris flows.

transport materials downslope, thereby forming a debris fan. Many flows are associated with deep beds of widely graded alluvial material, fed by tributary streams flowing in steep, rapidly eroding ravines. All these processes are controlled by the structure of the gully, and for this reason, the difference occurs between the tributary Menqian and Duo Zhao. Debris flow that occurred in the JJG almost came from Menqian instead of Duo Zhao and reasons can be summarized as follows: for material supplement, the Menqian Gully possesses about 60% of debris flow deposits; for topography, Menqian has a well-developed tree-shape water system constituting tributaries from lower to higher orders which contribute more to the occurrence of debris flows, while Duo Zhao has a braided drainage system with several channels of long stream length; for precipitation, data collected from rain gauges indicated that both frequency and amount of rainfall in Menqian is higher; from **Figure 2** and also field investigation, vegetation coverage in Menqian is less.

Precipitation and Debris Flow

Debris flow depends on the precipitation over the watershed; specifically, a surge depends on local rainfall and the corresponding material sources. At present, we consider only the gross coincidence between the rainfall and debris flow event, due to the lack of detailed data of local rainfall and material sources. In general, hydrological conditions leading to debris flow initiation may vary substantially, depending primarily on the rainfall pattern. High-magnitude rainfall may lead to soil saturation, reduce effective stress, and consequential slope instability, and finally generate debris flows (Milne et al., 2009). Given the material conditions of JJG, the debris flow is mainly controlled by the pattern and intensity of rainfall (including rainfall intensity–duration relationship, cumulative event rainfall, and antecedent rainfall, see Xiao-junGuo, 2013), and rainfall intensity is the major factor being considered in this research. A debris flow event here appears in a sequence of surges

within the duration of the rainfall event, with time intervals between surges about hundreds of seconds (Liu et al., 2009). **Table 1** lists eight events and the responsible rainfalls, in which the triggering intensity is identified as the intensity of rainfall from the rainfall start to the time of debris flow occurring and **Table 2** lists the elemental parameters of these events.

Statistical properties (e.g., the sum, mean, standard deviation, and maximum values) of the eight events are listed in **Table 3**, in which we also give the percentage of surge with discharge surplus 1/3 of the mean value. It is found that most events consist of “small” surges that have discharge below the 1/3 mean value; only two events, the 080705 and 170703 events, have more than half of surges that reach the 1/3 mean level. One finds no correlation between the overall rainfalls and the surge percentage of a certain discharge level, but the patterns of surge fluctuation exhibit some correlation to the rainfall patterns (**Figure 4**).

Figure 4 displays the rainfall and the associated debris flow event (the surge discharge fluctuation). This provides a gross coincidence between rainfall and debris flow. For example, a total of 33.3 mm was recorded on July 24, 2007, and the debris flow occurred at the maximum rainfall. The following day also witnessed debris flow at 13 o'clock with the triggering rainfall intensity of 8.2 mm/h.

All eight events occurred at the maximum rainfall intensity. The 130607 event has the highest (26.7 mm/h), occurring in the initial stage (the 3rd hour), followed by gradual decreasing rainfall intensity persisting about 7 h. Correspondingly, the surge discharges are relatively high in the early part. Most events (070724, 070725, 080705, 080711, and 170703) have relatively low triggering intensity (<10 mm/h) and mean intensity (<2 mm/h), that is the low-intensity long-duration rainfall pattern. The debris flow discharge pattern is directly influenced by the rainfall pattern. The most obvious example is the 070725 event, which has a similar outline with corresponding rainfall intensity.

TABLE 1 | Triggering rainfall events for the eight typical debris flows.

event date	Rainfall duration (h)	Mean intensity (mm/h)	Triggering intensity (mm/h)	Cumulative rainfall (mm)	Runoff (m ³)
2007.7.24	16	1.5	6.6	24	54715.9
2007.7.25	30	2.0	8.2	60.5	149425.0
2008.7.5	61	0.74	9.1	45.2	50956.9
2008.7.11	18	0.89	8.4	16	83250.7
2010.7.17	26	1.57	26.7	40.7	41655.8
2013.6.7	13	4.25	25.8	55.2	42323.1
2017.7.3	27	1.04	5.7	28	528285.6
2017.7.7	16	3.47	15	55.5	60808.4

TABLE 2 | Parameters for the eight debris flow events.

event	070724	070725	080705	080711	100717	130607	170703	170707
N	85	62	58	67	55	36	29	38
T _i	3:53	14:24	6:26	6:48	20:39	3:45	1:50	3:50
T _D (h)	9.1	3.93	5.57	7.2	3.33	6.25	4.67	5.17
ρ (g/cm ³)	2.0	2.15	2.15	2.16	2.12	2.14	2.14	2.16
Q _{max} (m ³ /s)	1358.3	2262.5	366.4	335	256.5	357	358.6	534.4
R _f (m ³ /s)	7046.6	22769.4	7614.9	6078.3	4036.4	3093.9	3629.0	3962.7
R _s (m ³)	39,672	109,072	37,944	95,736	36,277	45,484	387,053	57,766
H (m)	0.2–1.4	0.2–1.2	0.2–2.0	0.2–1.8	0.2–2.0	0.3–1.0	0.3–1.2	0.3–1.5
v (m/s)	3.95	5.74	6.87	6.01	7.30	4.95	6.22	7.68

Note: N, surge numbers of each debris flow; T_i, the debris flow initiating time; T_D, the debris flow duration; ρ, the debris flow density; Q_{max}, the maximum surge flux; R_f, the total flow amount of one debris flow event; R_s, the total sediment amount of one debris flow event; H, the thickness of debris flow; v, the mean velocity of debris flow.

TABLE 3 | Statistical values and >1/3 percentage of surge discharge series.

events	Mean	Sd	Max	>1/3 percentage
070724	82.9	200.24	1358.3	0.0353
070725	367.2	467.87	2262.5	0.1452
080705	131.3	98.14	366.4	0.5
080711	90.7	73.13	335	0.3432
100717	73.4	54.75	256.5	0.3091
130607	85.9	97.12	357	0.2778
170703	125.1	81.18	358.6	0.5862
170707	104.3	108.52	534.4	0.1579

The other events (170707, 070724, and 070725) have disperse peaks and especially a super peak surge. The 130607 event has rather high discharges in the former part, whereas the latter half shows rather low debris flow volumes.

Patterns of Surge Sequences

Each debris flow event in JJG lasts for several or dozens of hours and contains tens or even hundreds of surges separated in time (Cui, 2005). An event is a sequence of surges in a variety of appearances, thus we treat debris flow discharge series as time series. Based on the data, various patterns are found in the surge series, as shown in **Figure 5**, including single peak (070724), several single peaks (040721, three single peak), multi-peak (910711), single multi-peak (990716), and peak groups (910813). These five series are selected for their typical pattern performance.

Single (several single) peak series (070724 and 040721) always has little surges ($N < 100$) and represents precipitation because this event is characterized by short duration and low density. Multi-peak series (910711), especially several multi-peak series (910813), tend to have more surges ($N > 200$) that are induced by long duration and high-intensity rainfalls. The combination of single and multi-peak (990716) reflects more diverse rainfall information of this event, that is, during the former part (1–63 surges), overall rainfall intensity is rather low with just one moment bearing high intensity, while in the latter part (63–116), rainfall intensity stays at a rather high level.

Each debris flow event that occurs in the natural environment corresponds to one of these five types, and different types reflect different rainfall patterns. More examples of debris flow surge patterns can be seen in **Figure 6**.

Systematic Analysis of Debris Flow Events

To explore the temporal character of the surge series, especially the long-term memory and persistence nature of debris flows, we employ three time series analyzing methods: the Hurst exponent, the autocorrelation function (ACF), and the power spectrum analysis. The Hurst (1951) exponent, which is extensively used in hydrological and geophysical time series analysis, is employed to explore the long-range dependence of debris flow series. This parameter was calculated by the R/S analysis and has been used to investigate hydrological records of streamflow, precipitation (Miranda and Andrade, 1999), sea level (Beretta et al., 2005), paleo records of temperature (Rangarajan and Sant, 1997), etc.

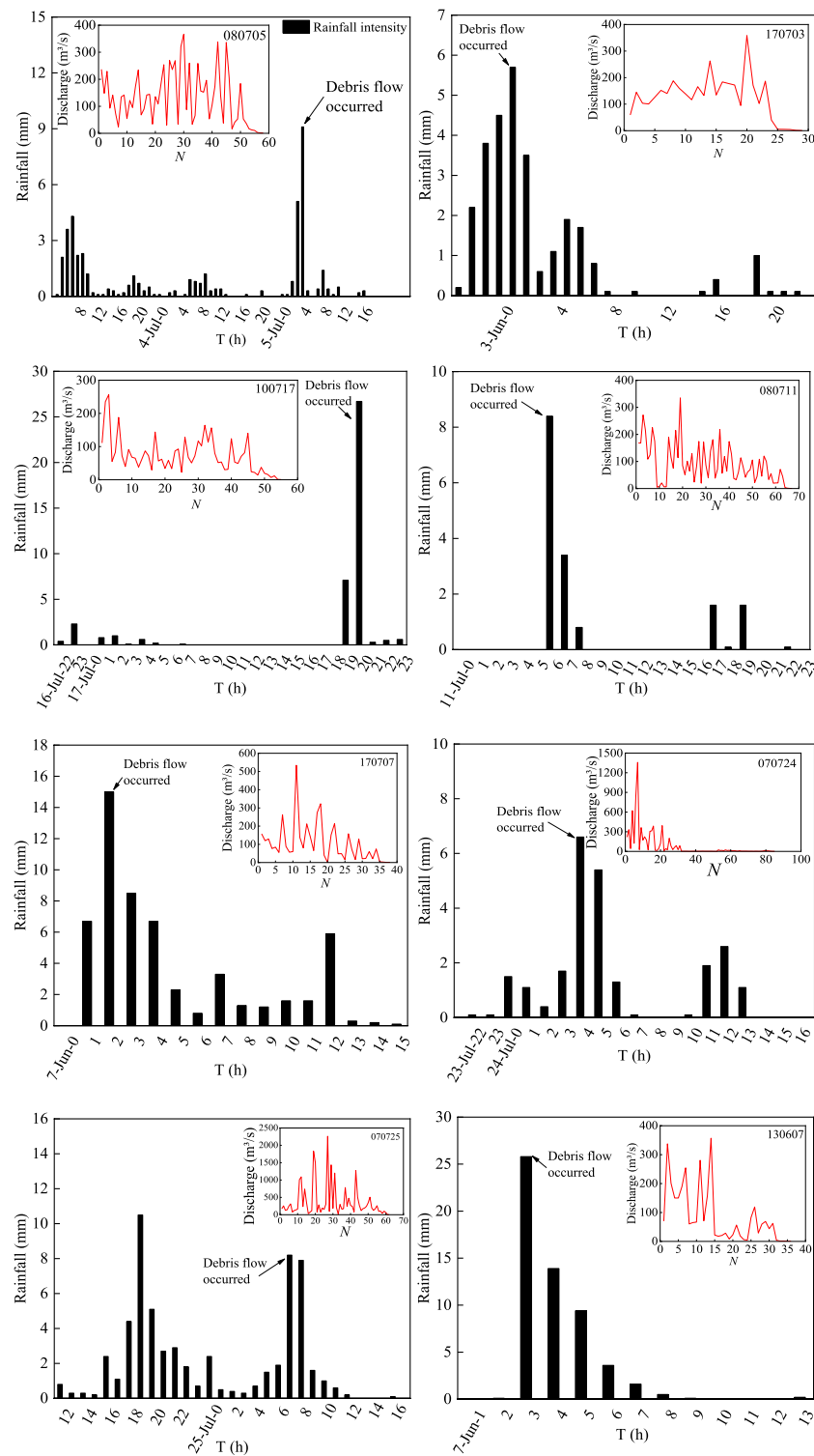


FIGURE 4 | Debris flows and corresponding rainfalls.

The ACF is a widely used theoretically and empirically robust statistical tool in geostatistics and ecology (Tobin, 2004). The power spectrum analysis is often seen in different kinds of time

series, such as series of soil moisture (Zhang et al., 2021), earth's gravity (Telesca et al., 2015), sonic velocity (Li, 2003), landslide, earthquake, and slope stability (Pelletier, 1997).

两个surge之间其实不存在连续的流动，
但是这样连成直线就有很强的误导性了

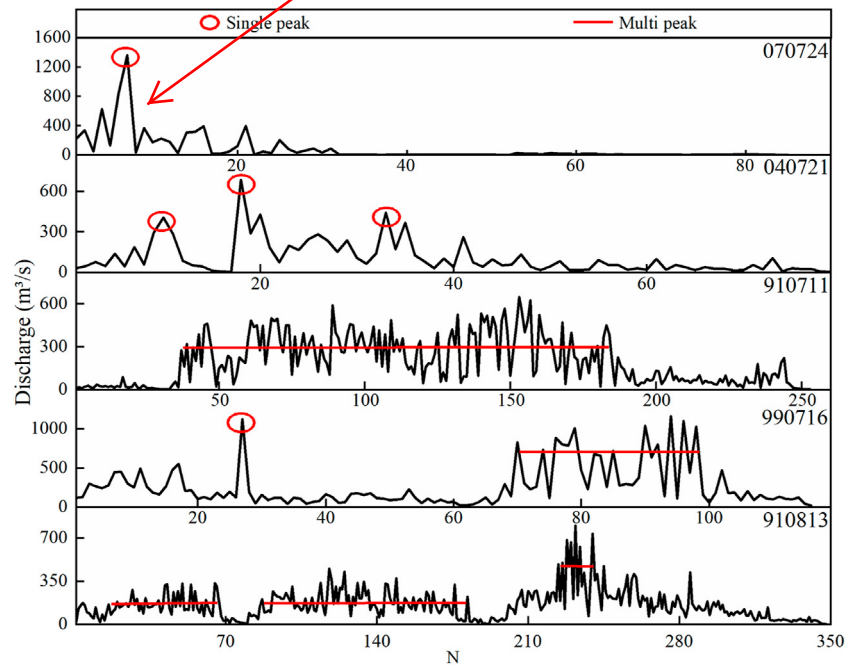


FIGURE 5 | Patterns of debris flow discharge fluctuation.

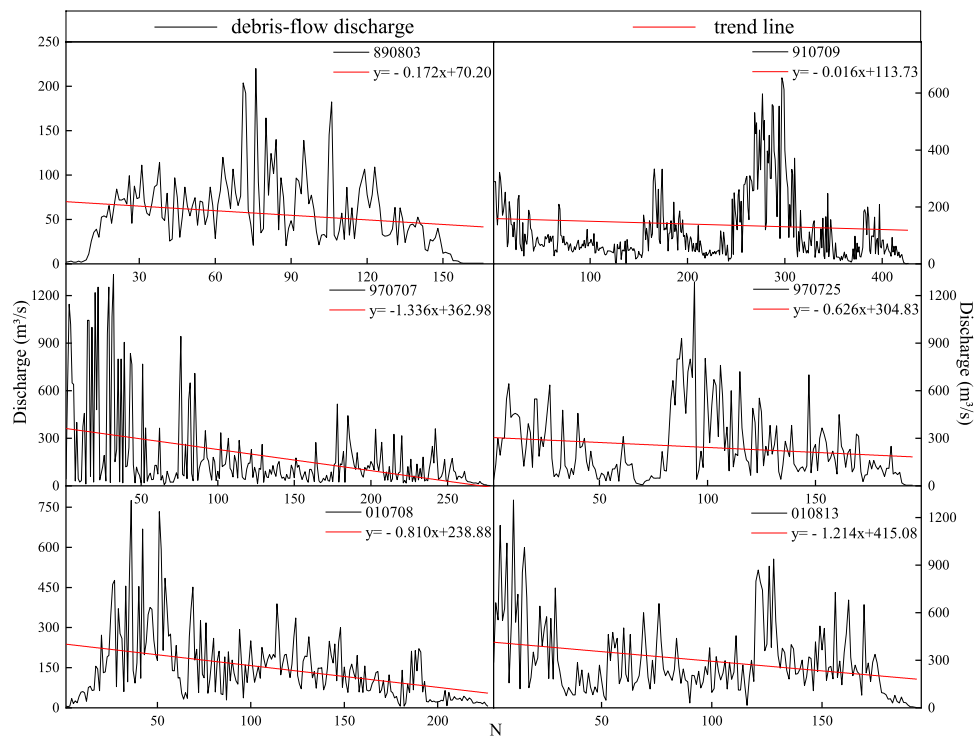
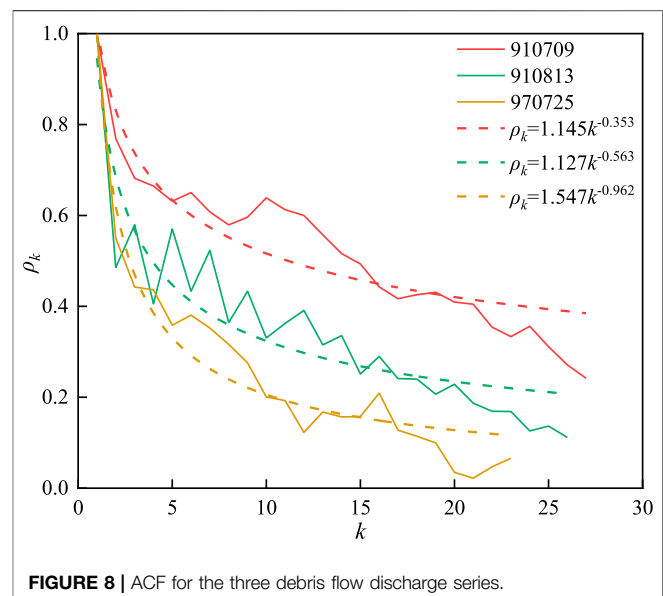
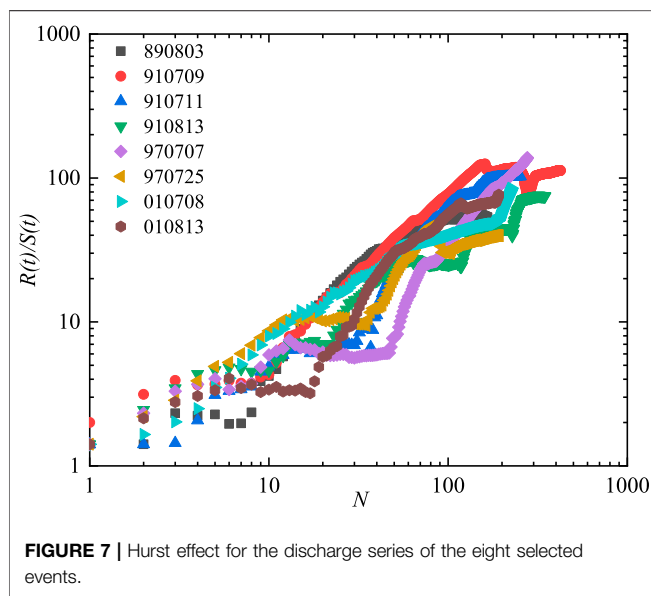


FIGURE 6 | More examples of debris flow surge patterns.

TABLE 4 | Hurst exponent values of different debris flow discharge series.

Events	N	H	$\bar{\rho}_k$	n	β	Events	N	H	$\bar{\rho}_k$	n	β
890627	120	0.9939	0.3258	0.745	1.756	010822	161	0.8199	0.1814	1.088	1.270
890802	129	0.9721	0.3396	0.379	1.880	020718	61	0.9350	0.2949	1.081	1.598
890803	166	0.9241	0.2693	0.801	1.643	020815	94	0.7713	0.1809	1.017	1.282
910709	427	0.9560	0.3184	0.353	1.612	020816	71	0.8072	0.2120	0.761	1.354
910711	253	0.9822	0.3821	0.334	1.880	020820	77	0.8122	0.1491	1.030	1.301
910813	348	0.8410	0.2218	0.563	1.346	030611	58	0.7301	0.1309	0.669	1.175
940616	154	0.8836	0.2418	0.563	1.436	030726	53	0.8966	0.2259	1.061	1.389
970707	278	0.8179	0.2175	0.504	1.367	030810	34	0.9917	0.3543	1.090	1.800
970715	127	0.7592	0.1294	0.805	1.232	040721	79	0.9083	0.2457	0.623	1.616
970725	194	0.8966	0.2535	0.962	1.422	040731	59	0.8227	0.1606	0.793	1.297
970829	95	0.9534	0.3406	0.659	1.777	040825	49	0.9061	0.2558	1.150	1.411
990716	116	0.9789	0.2985	1.142	1.715	050818	48	0.8934	0.2689	1.010	1.387
990724	89	0.9012	0.2774	0.751	1.589	070724	85	0.8631	0.2244	0.907	1.422
990810	68	0.8127	0.1739	1.155	1.367	070725	62	0.6521	0.0865	0.788	1.000
990816	148	0.8564	0.2059	0.799	1.440	080705	58	0.7804	0.1588	0.884	1.205
990818	78	0.8968	0.2949	0.535	1.460	080711	67	0.7228	0.1394	0.683	1.194
990825	83	0.9504	0.2784	1.063	1.689	100717	55	0.7056	0.1051	1.421	1.167
990829	146	0.9701	0.3656	0.535	1.663	130607	36	0.9072	0.2794	0.858	1.504
010708	227	0.9163	0.3031	0.520	1.633	170703	29	0.8383	0.1695	0.724	1.301
010813	193	0.8010	0.1840	1.384	1.243	170707	38	0.7840	0.1438	0.597	1.219



The Hurst Exponent

In this part, the Hurst exponent (H), first proposed by the British hydrologist Hurst (1956), was applied to analyze the long-term memory of debris flow discharge series. Detailed descriptions of the R/S analysis are as follows (Li et al., 2009):

Given a time series $\{\xi(t)\}$ $t = 1, 2, \dots, n$, divide the time series into τ subseries $\xi(t)$.

$$\langle \xi \rangle_\tau = \frac{1}{\tau} \sum_{t=1}^{\tau} \xi(t) \quad \tau = 1, 2, \dots \quad (1)$$

$$X(t, \tau) = \sum_{u=1}^t (\xi(u) - \langle \xi \rangle_\tau) \quad 1 \leq t \leq \tau \quad (2)$$

$$R(\tau) = \max_{1 \leq t \leq \tau} X(t, \tau) - \min_{1 \leq t \leq \tau} X(t, \tau) \quad \tau = 1, 2, \dots \quad (3)$$

$$S(\tau) = \left[\frac{1}{\tau} \sum_{t=1}^{\tau} (\xi(t) - \langle \xi \rangle_\tau)^2 \right]^{\frac{1}{2}} \quad \tau = 1, 2, \dots \quad (4)$$

$$R/S(\tau) = R(\tau)/S(\tau), \quad (5)$$

where $\langle \xi \rangle_\tau$ is the mean sequence of the time series; $X(t, \tau)$ is the cumulative deviation; $R(\tau)$ is the range; $S(\tau)$ is the standard deviation. If $R/S \propto \tau^H$, the time series shows the Hurst phenomenon, and the H value is called the Hurst exponent, which can be obtained by the least squares fitting in the double logarithmic coordinate system.

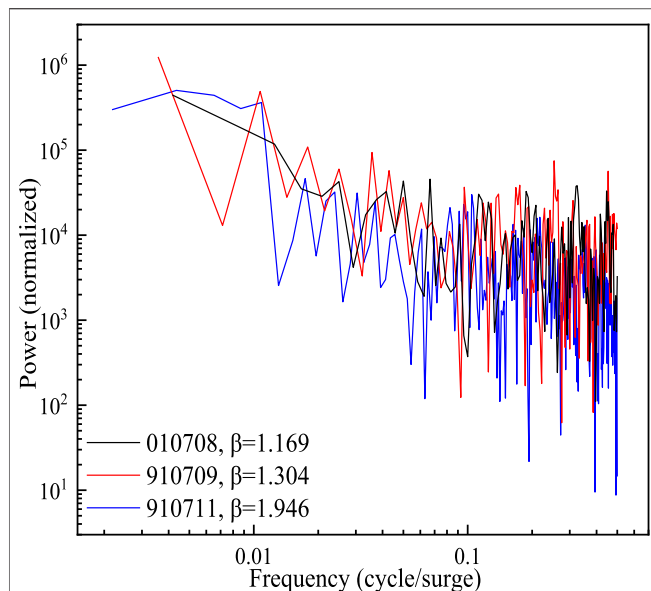


FIGURE 9 | The power spectrum of the three selected debris flow discharge series.

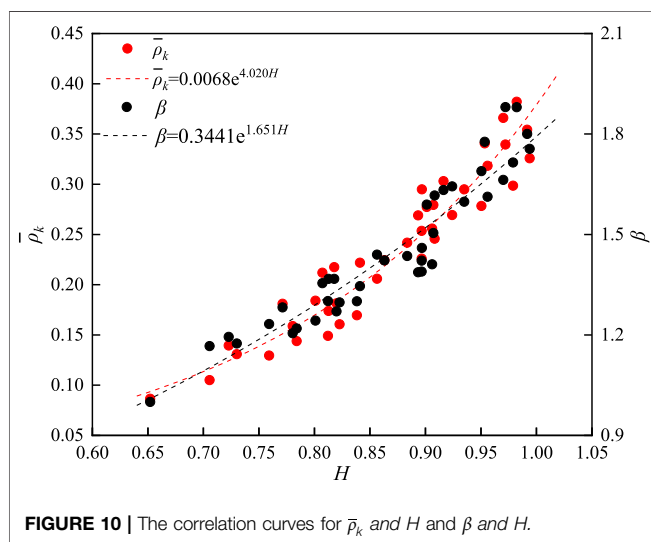


FIGURE 10 | The correlation curves for $\bar{\rho}_k$ and H and β and H .

The value of Hurst exponent H ranges from 0 to 1 (Rangarajan and Sant, 1997). When $H > 0.5$, the series has persistence or long-term memory, meaning the same trend in the series, with a greater value for more persistence; when $H = 0.5$, the series is random without persistence; and when $H < 0.5$, the series has anti-persistence or short term memory, and small H means high anti-persistence sustainability (Yin et al., 2009). The $R(t)/S(t)$ curves for the above-selected events are displayed in Figure 7 (the eight events being selected and displayed in the figure is that the Hurst exponent values of them rank the former eighth), showing a straight line in log-log plot with a slope higher than 45° . This means that the existence of Hurst exponent and $H > 0.5$. Similarly, we calculate H values for other sequences and all prove to be higher than 0.5, meaning the persistence of the sequences (see Table 4).

The Autocorrelation Function

The ACF also measures the persistence and anti-persistence nature of time series which is defined as (Akritas et al., 2014):

$$\hat{\rho}_k = \frac{\sum_{t=1}^{n-k} (x_t - \bar{x})(x_{t+k} - \bar{x})}{\sum_{t=1}^n (x_t - \bar{x})^2}, \quad (6)$$

where $\hat{\rho}_k$ is the autocorrelation exponent and $\bar{x}$ is the mean value of the sequence, $x_1, \dots, x_n$ (here is the discharge). x_t and x_{t+k} represent debris flow discharge values in the t and $t+k$ surge sequence, respectively.

Three examples of ACF are displayed in Figure 8. It is found that all the ACF decays with surge progress in a power-law form, $\rho_k \sim k^{-n}$ (with exponent n listed in Table 4). This means that the correlated range between surges in each event decreases rapidly, meaning that the memory is relatively short, ranging only within the first several or tens of surges.

The Power Spectrum

The power spectrum is another measure for the persistence and memory of time series. The power spectral density function (Jun, et al., 2021) is as follows:

$$S(f) \sim f^{-\beta}. \quad (7)$$

Here, the power spectrum S is the square of the Fourier coefficients at each wavenumber of a Fourier series (Malamud and Turcotte, 1999), and as for debris flow series, it represents the contribution of discharge along with different surges range (or fluctuation frequency). When $\beta > 1$, it represents the series has strong persistence or long-term memory character; $0 < \beta < 1$ indicates weak persistence or short memory (Parada et al., 2003). We calculated β values (Table 4) for all the debris flow series and three were selected and displayed in Figure 9 for they have different representative β values: 1.169 (010708), 1.304 (910709), and 1.946 (910711).

As $\beta > 1.0$, it means these events bear long-term memory and strong persistence character, in agreement with results that we got from the Hurst and ACF analysis.

The Correlation Between the Sequence Parameters

As the three parameters being mentioned above reflect the same nature of debris flows, in this part, we explore relationship of this three. We calculated the Hurst (H) values, the mean values of $\bar{\rho}_k$ (mean ACF), the n values, and the β values for the 40 debris flow discharge sequences (Table 4).

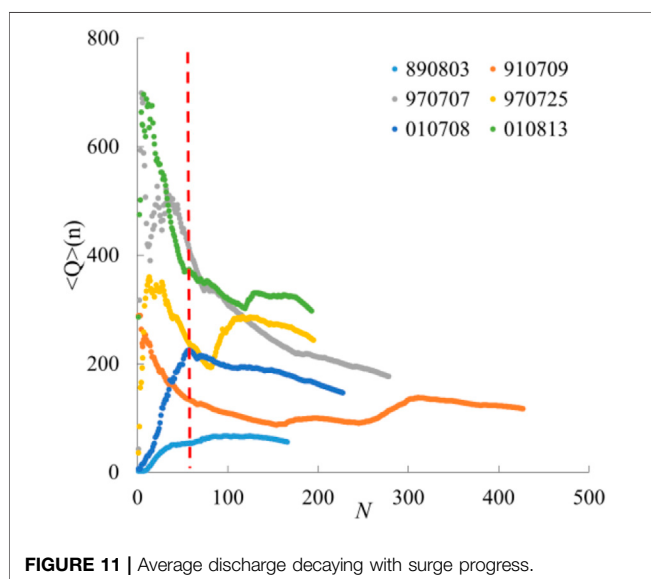
From the first sight of Table 4, both the mean ACF and β parameters have a close positive correlation with the Hurst exponent. All Hurst exponents and β values higher than 0.5 and 1.0, respectively, reflect the same long-term memory characteristic of debris flows. The n values (range between 0.334 and 1.421), however, have no obvious relationship with the Hurst exponent. Following, we quantify the relationship between $\bar{\rho}_k$ and H , β and H (see Figure 10).

As can be seen from the figure above, both $\bar{\rho}_k$ and β have exponential relationships with H , and the equations are displayed in Figure 9. Through in-depth investigation between these three

TABLE 5 | M-K trend parameters for the surge discharge sequences.

No	P	Stationary	Z	Trend	No	P	Stationary	Z	Trend
890627	0.010	Y	-6.740	↓*	010822	0.120	N	-0.795	↓
890802	0.049	Y	-7.554	↓	020718	0.093	N	-5.924	↓*
890803	0.161	N	-3.683	↓*	020815	0.076	N	-5.478	↓*
910709	0.357	N	-3.735	↓*	020816	0.046	N	-5.674	↓
910711	0.532	N	-1.545	↓	020820	0.573	N	-0.831	↓
910813	0.341	N	-2.521	↓	030611	0.010	Y	-3.961	↓
940616	0.010	Y	-7.082	↓*	030726	0.219	N	-4.472	↓*
970707	0.010	Y	-5.382	↓*	030810	0.651	N	-5.574	↓*
970715	0.018	N	-3.535	↓*	040721	0.010	Y	-4.945	↓*
970725	0.266	N	-2.856	↓*	040731	0.339	N	-3.885	↓*
970829	0.373	N	-3.970	↓*	040825	0.481	N	-3.465	↓*
990716	0.483	N	-0.260	↓	050818	0.086	N	-3.413	↓*
990724	0.160	N	-6.463	↓*	070724	0.350	N	-6.165	↓*
990810	0.270	N	-3.933	↓*	070725	0.010	Y	-1.482	↓
990816	0.010	Y	-2.976	↓*	080705	0.616	N	-2.355	↓
990818	0.010	Y	-7.533	↓*	080711	0.114	N	-3.989	↓*
990825	0.634	N	-1.734	↓	100717	0.368	N	-4.007	↓*
990829	0.2000	N	-8.386	↓*	130607	0.376	N	-4.359	↓*
010708	0.023	N	-7.029	↓	170703	0.915	N	-1.407	↓
010813	0.156	N	-3.454	↓*	170707	0.450	N	-3.445	↓*

Note: Z, Mann-Kendall Trend Test parameter; P, ADF parameter; ↓*, downward and obvious trend; ↓, downward but not obvious trend.

**FIGURE 11** | Average discharge decaying with surge progress.

parameters ($\bar{p}_k$, H , β) and rainfall parameters (i.e., mean, intriguing, and cumulative rainfall) no obvious correlation was obtained.

Trend Analysis of the Surge Series

We cite the Mann-Kendall trend test for tendency analysis of flow series. When $Z > 0$, the series displays an upward tendency, while $Z < 0$ indicates a downward tendency. For this test, if $p > 0.01$, we accept the null hypothesis, that is the series has no obvious tendency; if $p < 0.01$, we reject the null hypothesis, the trend is obvious. Meanwhile, the ADF (Augmented Dickey-Fuller Test, P) method is used to evaluate the stationary character of the debris flow series. The result of this method is P, and if $P < 0.05$, this series is treated to be a stationary one; if $P > 0.05$, reflects a nonstationary character of the

series. Results of these two methods for the 40 debris flow series are summarized in **Table 5**. There exists eight events in 40 debris flow series that have stationary character; in other words, most surge events are nonstationary. All debris flow series bear a downward tendency, among which 27 have an obvious trend.

The decaying or downward trend of debris flow discharge is more clearly illustrated by the moving average $\langle Q \rangle_n$ defined as follows:

$$\langle Q \rangle_n = (Q_1 + Q_2 + \dots + Q_n)/n. \quad (8)$$

It is found that $\langle Q \rangle_n$ is exclusively inclined to decrease in a power-law form after certain surge sequence (**Figure 11**) despite abrupt rising in the early episode.

Despite various surge peak types these events have, all series have a downward tendency, which is in accordance with results from Liu et al. (2009). That is to say, with time passing by, the inner energy that debris flows possess drops gradually. In particular, comparing with the corresponding rainfalls, one finds that the decaying tendency does not rely upon the pattern or quantity of rainfall. This means that the decaying is an intrinsic property of the surge sequence, which depends on the mass supplies in the watershed but not on the triggering rainfalls.

CONCLUSION

Surge waves are found to be ubiquitous of debris flow all over the world; their occurrences depend on the local conditions of material sources and rainfalls. In particular, field surveys and observations in JJG indicate that the surges within a debris flow event actually originate from different sources governed by local conditions of rainfall and morphology. As each debris flow event consists of tens or hundreds of surges, it must cover a wide range of mechanisms and patterns of flow initiation and development, and the underlying

mechanism is encoded in the properties of the surge sequence of the event. We have investigated the temporal characteristics of the surge sequences in JJG and come to the following conclusions:

1. Debris flows are of high variability in a watershed, depending on conditions of rainfall and material source distribution, which result in successive surges of various flow regimes and properties, presenting different fluctuation patterns of surge sequence.
2. Surge sequences of different debris flow events present similar properties of time series. The Hurst exponent, the ACF, and the power spectrum analysis prove that all the events bear long-term memory, implying the successive surges are not independent but correlated to some extent. Moreover, these three parameters are found to be interrelated in the form of the exponential function, with values depending on the respective rainfalls.
3. The sequences of surge discharge series appear as a gross trend of decay with the progress, despite patterns of surge sequences and rainfall processes. This implies the whole process of a debris flow is not completely dependent on the triggering rainfall but mainly on the intrinsic nature of material supplies controlled by the watershed.

These findings are important for understanding the forming and developing of debris flow in the watershed. In previous studies, a watershed is usually assumed to have certain debris flow occurrence in response to the triggering rainfall without considering the phenomena of separate surges and the

fluctuation of surge sequence. This research suggests that a complete theory of debris flow should establish mechanisms and provide an explanatory framework for the intermittency and variability of surges, which will be heuristic in prompting the studies in evaluation and engineering prevention of debris flow.

DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

AUTHOR CONTRIBUTIONS

JZ produced the figures and wrote the manuscript. YL was responsible for the main idea of the manuscript and contributed to the manuscript revision. XG, BY, TY, and DL provided input to figure and text editing. All the authors contributed to the article and approved the submitted version.

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